

Seminar Title : Superlinear and Sublinear Dirichlet problem with the  $(p(y),q(y))$ -Laplacian Operator

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Abstract : We study the following nonlinear elliptic problem involving the  $(p(y),q(y))$ -Laplacian Operator:  $-\operatorname{div}(a(y)|\nabla v|^{p(y)-2} \nabla v) + b(y)|v|^{p(y)-2} v - \operatorname{div}(|v|^{q(y)-2} \nabla v) = g(y,v)$   $y \in \Omega$ ,  $v = 0$  on  $\partial\Omega$ , where  $\Omega \subset \mathbb{R}^n$  is a smooth bounded domain,  $1 < q(y) < p(y) < n$ . The functions  $a, b \in L^\infty(\Omega)$  and  $a(y) \geq a_0 > 0$ ,  $b(y) \geq b_0 > 0$  for all  $y \in \Omega$ . We prove the existence of weak solutions in  $W_0^{1,p(\cdot)}$ ,  $W_0^{1,q(\cdot)}(\Omega)$  for the superlinear case  $g(y,v) = h(y) |v|^\beta$ ,  $p(y) - 1 < \beta < p^*(y) - 1$ , and sublinear case  $g(y,v) = f(y) |v|^\alpha$ ,  $0 \leq \alpha < q(y) < p(y) - 1$ , by using the Mountain Pass Theorem.